

Matrices & Systems of Equations (8) Conic Sections (10)

Selected Examples:

1. Find the vertex and focus for the parabola:

$$x^2 - 10x + 12y + 37 = 0$$

2. Find the vertices and foci for the ellipse:

$$\frac{(x-1)^2}{16} + \frac{(y+2)^2}{7} = 1$$

Practice:

Determinants (8)	1. Find the Determinant: $\begin{bmatrix} 3 & -8 \\ 12 & -4 \end{bmatrix}$	2. Find the determinant: $\begin{bmatrix} 1 & 4 & -2 \\ 3 & -1 & 1 \\ 5 & 2 & 7 \end{bmatrix}$
Area using Determinants (8)	3. Use determinants to find the area of triangle with vertices (0,3), (4, -1) and (-3,2) .	
Solving Systems (8) - Gaussian Elimination - Gauss-Jordan Elimination - Using an Inverse Matrix - Cramer's Rule	4. Solve the system of equations: $\begin{array}{rcl} 2x & +3y & -4z = 4 \\ x & -y & -5z = 0 \\ -2x & +4y & +5z = 9 \end{array}$	
Circle (10)	5. Find the center and radius: $x^2 + y^2 + 6x - 2y + 1 = 0$.	
Parabola (10)	6. Find the vertex, focus, and directrix: $y^2 - 6y - 12x - 15 = 0$.	
Ellipse (10)	7. Find the center, vertices, foci, and eccentricity: $\frac{(x+1)^2}{64} + \frac{(y-4)^2}{36} = 1$.	
Hyperbola (10)	8. Find the center, vertices, foci, and asymptotes: $\frac{(y+2)^2}{4} - \frac{(x)^2}{12} = 1$.	

Mixed Review

9. Vector \mathbf{v} has initial point $(-4, 5)$ and final point $(9, 1)$. Write vector \mathbf{v} in component form and in linear combination form.

10. Convert to polar form: $(4, -4\sqrt{3})$

11. Find the area of a triangle with side lengths $\{8, 4, 10\}$.

12. Use DeMoivre's Theorem to evaluate $(-2 + 2\sqrt{3}i)^3$ in standard form.

13. Solve for x : $\ln(x) + \ln(2x + 8) = \ln(90)$

14. State the domain: $y = \frac{3x}{\sqrt{3x+9}}$

Mixed Review

1. State the vertical and horizontal asymptotes of $f(x) = \frac{3x^2 - 2x + 4}{x^2 - 8x + 15}$.

2. Divide synthetically: $(x^4 + 2x^2 - x + 1) \div (x + 2)$

3. Factor: $x^4 + 2x^3 + x^2 + 2x$

4. Solve: $e^{4x+1} = 9$

5. Convert to polar form: $(6, -6\sqrt{3})$

6. Find the foci and eccentricity for the ellipse: $\frac{x^2}{28} + \frac{y^2}{64} = 1$.

7. $\sin u = \frac{5}{14}$, $\tan u < 0$ find $\sin 2u$. (in simplest radical form)

8. Use DeMoivre's Theorem to evaluate: $(3 - 3i)^3$

9. Find the determinant:
$$\begin{bmatrix} 1 & 9 & -1 \\ -6 & 3 & 8 \\ 0 & 4 & 5 \end{bmatrix}$$

10. Evaluate: a) $\sum_1^{50} 48i - 3$ b) $\sum_1^{\infty} \left(\frac{3}{4}\right)^{i-1}$

11. Find the area of a triangle with:
a. Sides lengths {20, 25, 30} b. Vertices: (5,6), (3, -4), (9, 1)

12. Vector v has initial point (5, 7) and final point (-4, 9). Write v in:
a. Component form
b. Linear Combination Form
c. Trigonometric Form

Mixed Review

1. State the amplitude, period and shifts of the graph of $y = 2\cos(6x - \pi) + 4$

2. Solve on $(0, 2\pi]$: $6\cos^2 x - 5\sin x - 2 = 0$

3. Evaluate: $\cos(135^\circ + 60^\circ)$. (in simplest radical form)

4. Solve: $\log(7 - x) - \log(3x + 2) = 1$

5. Find a formula, a_n , for an arithmetic sequence with $a_4 = 3$ and $a_{15} = 47$.

6. Lucy invests \$900 at a rate of 1.5% compounded continuously. What is her balance after 15 years?

7. Find the composition $f(g(x))$:
 $f(x) = 3x^2 - 7$
 $g(x) = \sqrt{2x + 1}$

8. State the Domain: $y = x^2 - 7x$

9. $f(x) = 4x^3 - 8x^2 - 25x + 50$ State the number of possible *positive real zeros* of $f(x)$ and list all possible *rational zeros*.

10. Factor: $8x^3 + 1$

11. Solve: $2x^2 - 5x = x^2 + 1$

12. Find the inverse: $f(x) = 3x^2 - 7$

13. Solve the system:
 $2x - y + z = -3$
 $x + y + z = 4$
 $3x - 2y + 5z = 1$

14. Write the equation of $g(x)$, which is $f(x)=x^2$ shifted 3 units up and 5 units left.

15. Find the modulus and argument for the complex number $z = -5 + 5i$.

